

Evaluate the following limits. **Must show work!** Reduce answer when possible. Remember to write the limit notation as you work.

1. $\lim_{x \rightarrow 3} \frac{x-3}{x^3-27} = \frac{1}{27}$
 $f(3) = \frac{0}{0}$ Indeterminate
 $\lim_{x \rightarrow 3} \frac{(x-3)}{(x-3)(x^2+3x+9)}$
 $\lim_{x \rightarrow 3} \frac{1}{x^2+3x+9} = \frac{1}{3^2+3(3)+9} = \frac{1}{27}$

2. $\lim_{x \rightarrow 3} \frac{\frac{1}{x} + \frac{1}{3}}{x-3} = \text{DNE}$
 $(3x)\frac{1}{x} + \frac{1}{3}(3x)$
 $\frac{3+x}{(x-3)(3x)}$
 $f(3) = \frac{\frac{1}{3} + \frac{1}{3}}{3-3} = \frac{\frac{2}{3}}{0}$
 Test pts

$x = 2.99$	3.01
$\frac{1}{x}$	$\frac{1}{x}$
$-\infty$	$+\infty$

3. $\lim_{x \rightarrow -4} \frac{\frac{1}{4} - \frac{1}{x}}{4+x} = \text{DNE}$
 $\frac{\frac{1}{4} - (\frac{1}{-4})}{4+(-4)} = \frac{\frac{1}{2}}{0}$
 $\frac{(\frac{1}{4} - \frac{1}{x})(4x)}{(4+x)(4x)}$
 $\frac{x-4}{4x(x+4)}$

4. $\lim_{x \rightarrow -2} \frac{x^2-4}{x^2-6x-16} = \frac{2}{5}$
 $f(-2) = \frac{(-2)^2-4}{(-2)^2-6(-2)-16} = \frac{0}{0}$
 $\frac{(x+2)(x-2)}{(x-8)(x+2)}$
 $\lim_{x \rightarrow -2} \frac{x-2}{x-8} = \frac{-2-2}{-2-8} = \frac{-4}{-10} = \frac{2}{5}$

$x =$

-4.01	-3.99
$\frac{1}{x}$	$\frac{1}{x}$
$-\infty$	$+\infty$

5. $\lim_{x \rightarrow 16} \frac{\sqrt{x}-4}{x-16} = \frac{1}{8}$
 $f(16) = \frac{\sqrt{16}-4}{16-16} = \frac{0}{0}$
 $\lim_{x \rightarrow 16} \frac{\sqrt{x}-4}{x-16} \cdot \frac{\sqrt{x}+4}{\sqrt{x}+4}$
 $\lim_{x \rightarrow 16} \frac{x-16}{(x-16)(\sqrt{x}+4)} = \frac{1}{\sqrt{16}+4} = \frac{1}{4+4}$

6. $\lim_{x \rightarrow 0} \frac{x}{\sqrt{x+9}-3} = 6$
 $f(0) = \frac{0}{\sqrt{9}-3} = \frac{0}{0}$
 $\lim_{x \rightarrow 0} \frac{x}{\sqrt{x+9}-3} \cdot \frac{\sqrt{x+9}+3}{\sqrt{x+9}+3}$
 $\lim_{x \rightarrow 0} \frac{x(\sqrt{x+9}+3)}{x+9-9} = \lim_{x \rightarrow 0} \frac{\sqrt{x+9}+3}{\sqrt{0+9}+3}$

Without Graphing Evaluate Given:

$$g(x) = \begin{cases} |x| & , x \leq -1 \\ 2x - 1 & , -1 < x \leq 1 \\ x^2 & , x > 1 \end{cases}$$

7. $\lim_{x \rightarrow 1^+} g(x) = 1^2 = 1$

8. $\lim_{x \rightarrow 1^-} g(x) = 2(1) - 1 = 1$

9. $\lim_{x \rightarrow 1} g(x) = 1$

10. $\lim_{x \rightarrow 5} g(x) = 5^2 = 25$

11. $\lim_{x \rightarrow -1^+} g(x) = 2(-1) - 1 = -3$

12. $\lim_{x \rightarrow -1^-} g(x) = |-1| = 1$

13. $\lim_{x \rightarrow -1} g(x) = \text{DNE}$
 $\lim_{x \rightarrow -1^+} g(x) \neq \lim_{x \rightarrow -1^-} g(x)$

14. $\lim_{x \rightarrow 0} g(x) = 2(0) - 1 = -1$