

3.5 p. 146-147

$$1) y = 1 + x - \cos x$$

$$y' = 1 - (-\sin x)$$

$$y' = 1 + \sin x$$

$$3) y = \frac{1}{x} + 5 \sin x$$

$$y = x^{-1} + 5 \sin x$$

$$y' = -x^{-2} + 5 \cos x = -\frac{1}{x^2} + 5 \cos x$$

$$5) y = 4 - x^2 \sin x$$

$$y' = -x^2(\cos x) + \sin x(-2x) = \boxed{-x^2 \cos x - 2x \sin x}$$

$$7) y = \frac{4}{\cos x} = 4 \sec x$$

$$y' = \boxed{4 \sec x \tan x}$$

If Quotient Rule

$$y' = \frac{\cos x (0) - 4(-\sin x)}{\cos^2 x}$$

$$= \frac{4 \sin x}{\cos^2 x}$$

$$y' = 4 \frac{\sin x}{\cos x} \cdot \frac{1}{\cos x}$$

$$9) y = \frac{\cot x}{1 + \cot x}$$

$$y' = \frac{(1 + \cot x)(-\csc^2 x) - \cot x(-\csc^2 x)}{(1 + \cot x)^2}$$

y

$$y' = \frac{-\csc^2 x (1 + \cot x - \cot x)}{(1 + \cot x)^2}$$

$$? \quad y' = \boxed{-\frac{\csc^2 x}{(1 + \cot x)^2}} = -\frac{1}{(\sin x + \cos x)^2}$$

$$21) \quad y = \sin x + 3 \text{ at } x = \pi \quad y(\pi) = \sin \pi + 3 = 3$$

$$y' = \cos x \quad (\pi, 3)$$

$$y'(\pi) = \cos \pi = -1$$

$$m_{\text{Tan}} = -1$$

$$m_{\text{Nor}} = 1$$

$$\text{Tangent } \boxed{y - 3 = -(x - \pi)}$$

$$y = -x + \pi + 3$$

$$\text{Normal } \boxed{y - 3 = (x - \pi)}$$

$$y = x - \pi + 3$$

$$31) \quad y = 4 + \cot x - 2 \csc x$$

$$y' = -\csc^2 x - 2(-\csc x \cot x)$$

$$y' = -\csc^2 x + 2 \csc x \cot x$$

a) tangent to curve at

$$P\left(\frac{\pi}{2}, 2\right)$$

$$y'\left(\frac{\pi}{2}\right) = -\left(\csc \frac{\pi}{2}\right)^2 + 2 \csc \frac{\pi}{2} \cot \frac{\pi}{2}$$

$$= -(1)^2 + 2(1)(0) = \boxed{-1}$$

$$\boxed{y - 2 = -(x - \frac{\pi}{2})}$$

$$y = -x + \frac{\pi}{2} + 2$$

b) Horizontal tangent at Q.

$$0 = -\csc^2 x + 2 \csc x \cot x$$

$$0 = -\csc x (\csc x - 2 \cot x)$$

$$0 = -\csc x \left(\frac{1}{\sin x} - \frac{2 \cos x}{\sin x} \right)$$

$$-\csc x = 0 \quad \frac{1 + 2 \cos x}{\sin x} = 0$$

$$-\frac{1}{\sin x} = 0$$

$$1 - 2 \cos x = 0$$

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$$\cos x = \frac{1}{2}$$

$$x = \frac{\pi}{3}$$

$$y\left(\frac{\pi}{3}\right) = 4 + \cot \frac{\pi}{3} - 2 \csc \frac{\pi}{3}$$

$$= 4 + \frac{\sqrt{3}}{3} - 2\left(\frac{2\sqrt{3}}{3}\right)$$

$$4 - \frac{\sqrt{3}}{3} = 4 - \sqrt{3}$$

$$\left(\frac{\pi}{3}, 4 - \sqrt{3}\right)$$

$$\boxed{y = 4 - \sqrt{3}}$$

47) Which is an equation of the normal line to $y = \sin x + \cos x$ at $x = \pi$.

$$y' = \cos x - \sin x$$

$$y'(\pi) = \cos \pi - \sin \pi$$

$$-1 - 0 = \boxed{-1}$$

$$y(\pi) = \sin \pi + \cos \pi$$

$$= 0 + (-1) = -1$$

$$(\pi, -1)$$

$$m_{\text{Nor}} = 1$$

$$y + 1 = 1(x - \pi)$$

\boxed{B}

$$y = x - \pi - 1$$

48) Find y'' if $y = x \sin x$

$$y' = x(\cos x) + \sin x(1)$$

$$y' = x \cos x + \sin x$$

$$y'' = x(-\sin x) + \cos x(1) + \cos x$$

$$\boxed{C} \quad y'' = -x \sin x + 2 \cos x$$