

3. $\int_1^2 \frac{1}{x^2} dx =$

(A) $-\frac{1}{2}$

(B) $\frac{7}{24}$

(C) $\frac{1}{2}$

(D) 1

(E) $2 \ln 2$

4. If f is continuous for $a \leq x \leq b$ and differentiable for $a < x < b$, which of the following could be false?

(A) $f'(c) = \frac{f(b) - f(a)}{b - a}$ for some c such that $a < c < b$.

(B) $f'(c) = 0$ for some c such that $a < c < b$.

(C) f has a minimum value on $a \leq x \leq b$.

(D) f has a maximum value on $a \leq x \leq b$.

(E) $\int_a^b f(x) dx$ exists.

5. $\int_0^x \sin t dt =$

(A) $\sin x$

(B) $-\cos x$

(C) $\cos x$

(D) $\cos x - 1$

(E) $1 - \cos x$

6. If $x^2 + xy = 10$, then when $x = 2$, $\frac{dy}{dx} =$

- (A) $-\frac{7}{2}$ (B) -2 (C) $\frac{2}{7}$ (D) $\frac{3}{2}$ (E) $\frac{7}{2}$
-

7. $\int_1^e \left(\frac{x^2 - 1}{x} \right) dx =$

- (A) $e - \frac{1}{e}$ (B) $e^2 - e$ (C) $\frac{e^2}{2} - e + \frac{1}{2}$ (D) $e^2 - 2$ (E) $\frac{e^2}{2} - \frac{3}{2}$
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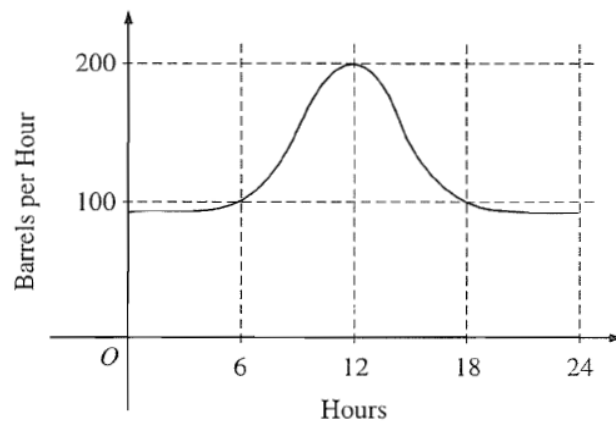
8. Let f and g be differentiable functions with the following properties:

(i) $g(x) > 0$ for all x

(ii) $f(0) = 1$

If $h(x) = f(x)g(x)$ and $h'(x) = f(x)g'(x)$, then $f(x) =$

- (A) $f'(x)$ (B) $g(x)$ (C) e^x (D) 0 (E) 1
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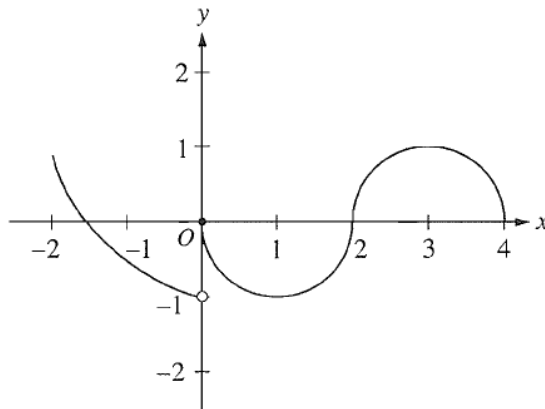
9. The flow of oil, in barrels per hour, through a pipeline on July 9 is given by the graph shown above. Of the following, which best approximates the total number of barrels of oil that passed through the pipeline that day?

- (A) 500 (B) 600 (C) 2,400 (D) 3,000 (E) 4,800

10. What is the instantaneous rate of change at $x = 2$ of the function f given by $f(x) = \frac{x^2 - 2}{x - 1}$?
- (A) -2 (B) $\frac{1}{6}$ (C) $\frac{1}{2}$ (D) 2 (E) 6
-

11. If f is a linear function and $0 < a < b$, then $\int_a^b f''(x) dx =$
- (A) 0 (B) 1 (C) $\frac{ab}{2}$ (D) $b - a$ (E) $\frac{b^2 - a^2}{2}$
-

12. If $f(x) = \begin{cases} \ln x & \text{for } 0 < x \leq 2 \\ x^2 \ln 2 & \text{for } 2 < x \leq 4, \end{cases}$ then $\lim_{x \rightarrow 2} f(x)$ is
- (A) $\ln 2$ (B) $\ln 8$ (C) $\ln 16$ (D) 4 (E) nonexistent
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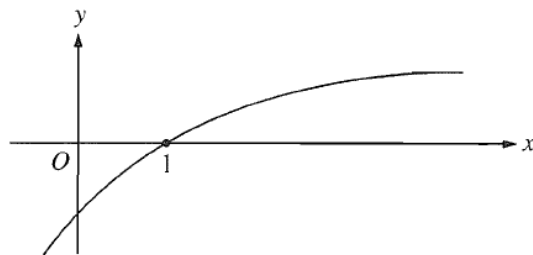


13. The graph of the function f shown in the figure above has a vertical tangent at the point $(2, 0)$ and horizontal tangents at the points $(1, -1)$ and $(3, 1)$. For what values of x , $-2 < x < 4$, is f not differentiable?
- (A) 0 only (B) 0 and 2 only (C) 1 and 3 only (D) $0, 1,$ and 3 only (E) $0, 1, 2,$ and 3

14. A particle moves along the x -axis so that its position at time t is given by $x(t) = t^2 - 6t + 5$. For what value of t is the velocity of the particle zero?
- (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

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15. If $F(x) = \int_0^x \sqrt{t^3 + 1} dt$, then $F'(2) =$
- (A) -3 (B) -2 (C) 2 (D) 3 (E) 18

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16. If $f(x) = \sin(e^{-x})$, then $f'(x) =$
- (A) $-\cos(e^{-x})$
(B) $\cos(e^{-x}) + e^{-x}$
(C) $\cos(e^{-x}) - e^{-x}$
(D) $e^{-x} \cos(e^{-x})$
(E) $-e^{-x} \cos(e^{-x})$



17. The graph of a twice-differentiable function f is shown in the figure above. Which of the following is true?
- (A) $f(1) < f'(1) < f''(1)$
(B) $f(1) < f''(1) < f'(1)$
(C) $f'(1) < f(1) < f''(1)$
(D) $f''(1) < f(1) < f'(1)$
(E) $f''(1) < f'(1) < f(1)$

18. An equation of the line tangent to the graph of $y = x + \cos x$ at the point $(0, 1)$ is

- (A) $y = 2x + 1$ (B) $y = x + 1$ (C) $y = x$ (D) $y = x - 1$ (E) $y = 0$
-

19. If $f''(x) = x(x + 1)(x - 2)^2$, then the graph of f has inflection points when $x =$

- (A) -1 only (B) 2 only (C) -1 and 0 only (D) -1 and 2 only (E) $-1, 0,$ and 2 only
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20. What are all values of k for which $\int_{-3}^k x^2 dx = 0$?

- (A) -3 (B) 0 (C) 3 (D) -3 and 3 (E) $-3, 0,$ and 3
-

21. If $\frac{dy}{dt} = ky$ and k is a nonzero constant, then y could be

- (A) $2e^{kty}$ (B) $2e^{kt}$ (C) $e^{kt} + 3$ (D) $kty + 5$ (E) $\frac{1}{2}ky^2 + \frac{1}{2}$
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22. The function f is given by $f(x) = x^4 + x^2 - 2$. On which of the following intervals is f increasing?

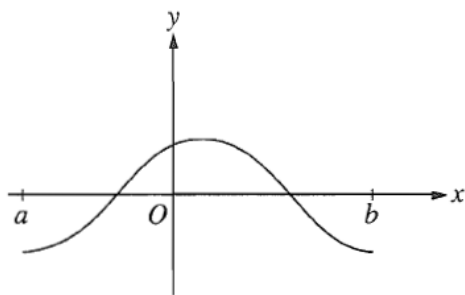
(A) $\left(-\frac{1}{\sqrt{2}}, \infty\right)$

(B) $\left(-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$

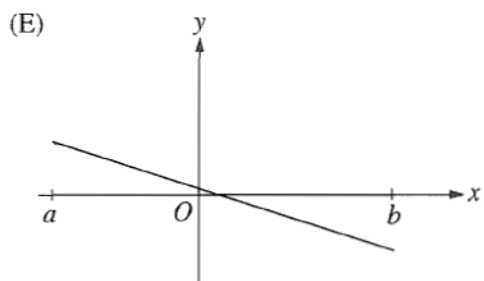
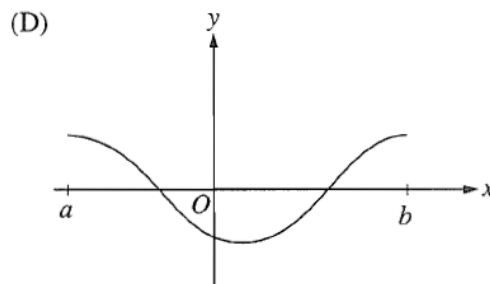
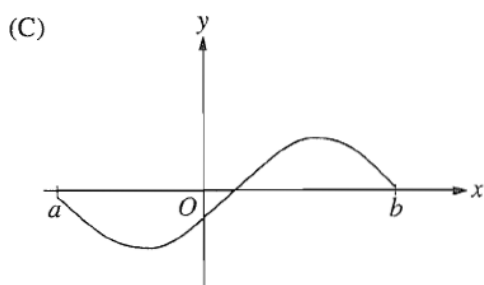
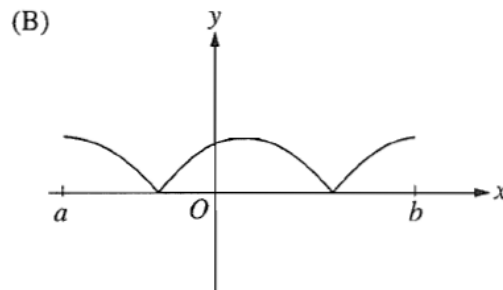
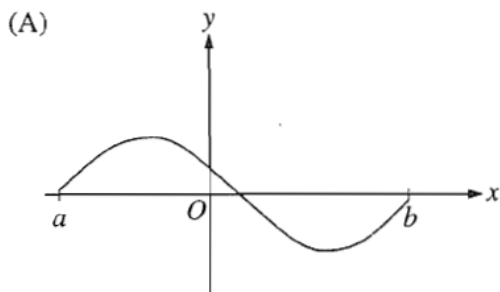
(C) $(0, \infty)$

(D) $(-\infty, 0)$

(E) $\left(-\infty, -\frac{1}{\sqrt{2}}\right)$



23. The graph of f is shown in the figure above. Which of the following could be the graph of the derivative of f ?



24. The maximum acceleration attained on the interval $0 \leq t \leq 3$ by the particle whose velocity is given by $v(t) = t^3 - 3t^2 + 12t + 4$ is
- (A) 9 (B) 12 (C) 14 (D) 21 (E) 40
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25. What is the area of the region between the graphs of $y = x^2$ and $y = -x$ from $x = 0$ to $x = 2$?
- (A) $\frac{2}{3}$ (B) $\frac{8}{3}$ (C) 4 (D) $\frac{14}{3}$ (E) $\frac{16}{3}$

x	0	1	2
$f(x)$	1	k	2

26. The function f is continuous on the closed interval $[0, 2]$ and has values that are given in the table above. The equation $f(x) = \frac{1}{2}$ must have at least two solutions in the interval $[0, 2]$ if $k =$
- (A) 0 (B) $\frac{1}{2}$ (C) 1 (D) 2 (E) 3
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27. What is the average value of $y = x^2\sqrt{x^3 + 1}$ on the interval $[0, 2]$?
- (A) $\frac{26}{9}$ (B) $\frac{52}{9}$ (C) $\frac{26}{3}$ (D) $\frac{52}{3}$ (E) 24

28. If $f(x) = \tan(2x)$, then $f'\left(\frac{\pi}{6}\right) =$
- (A) $\sqrt{3}$ (B) $2\sqrt{3}$ (C) 4 (D) $4\sqrt{3}$ (E) 8